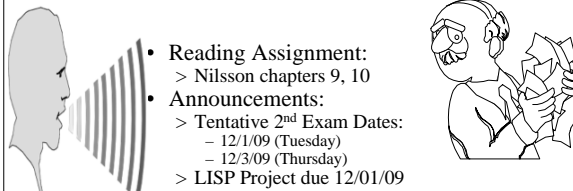


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## Announcements



- Reading Assignment:
  - > Nilsson chapters 9, 10
- Announcements:
  - > Tentative 2<sup>nd</sup> Exam Dates:
    - 12/1/09 (Tuesday)
    - 12/3/09 (Thursday)
  - > LISP Project due 12/01/09
- Today's Handouts in WWW:
  - > Outline Class 24
- Web Site
  - > [www.mil.ufl.edu/eel5840](http://www.mil.ufl.edu/eel5840)
  - > Software and Notes

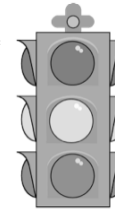
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## Today's Menu



- Finish up Heuristic Search (Chapter 9)
  - ⇒ Final Comments on the Admissibility of A\*
  - ⇒ IDA\* & RBFS
  - ⇒ Search Efficiency

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## Heuristic Searches

Related Algorithms

- Bi-Directional Search
  - > Breadth-First may expand less nodes bi-directionally than unidirectionally as shown in the Figure.
  - > However, if the  $h(n)$  used by the bidirectional process are slightly inaccurate, the search frontiers may not intersect.



(a) Breadth-first search



(b) Heuristic search

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## Heuristic Searches

Related Algorithms

- Staged Search : Prune the tree at some stages of computation in order to free up storage. At the end of each stage you keep only the most promising nodes (those with good  $f$  values). Obviously, staged search carries no guarantee of optimality
- Limitation of Successors - to keep  $\Gamma(n)$  small we also keep only the "best" nodes
  - > We will need additional problem domain knowledge (i.e., a DEADEND)
  - > We either modify A\* or assign to some nodes very high  $h(n)$  values
  - > Consider evaluating  $h(\Gamma(n))$  before evaluating the DBs themselves and only select those nodes with high promise

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**Heuristic Search**

- Iterative Deepening
  - Enjoys the same linear memory requirements of DFS while guaranteeing that a goal node of minimal depth will be found- memory grows linearly with the depth of the goal.
  - Successive depth-first searches are conducted-each with a depth bound increasing by 1-until a goal node is found.

Depth bound = 1      Depth bound = 2      Depth bound = 3      Depth bound = 4

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**Heuristic Search**

- How many nodes are expanded by BFS?  
 Assuming uniform branching factor  $b$ , with a goal at depth  $d$   
 $1 + b + b^2 + \dots + b^d = (b^{d+1} - 1)/(b - 1)$
- How many nodes are expanded by iterative deepening?  
 Down to level  $j$  we have  $N_{dfj} = (b^{j+1} - 1)/(b - 1)$   
 At worst, we must conduct  $d$  such searches for the goal at depth  $d$   
 $N_{id} = \sum_{j=0}^d (b^{j+1} - 1)/(b - 1) = (b^{d+2} - 2b - bd + d + 1)/(b - 1)^2$   
 for large  $d$  this reduces to  
 $N_{id}/N_{bf} = b/(b - 1)$   
 For  $b = 10$  and large  $d$  this is about 1.11% or ID expands about 11% more nodes than BFS

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**Heuristic Search**

- IDA\* (Korf, 1985)
  - > Allows us to find minimal cost paths with memory that grows linearly with the depth of the goal.
  - > Execute a series of depth-first searches. In the first search we establish a cost cutoff equal to  $f(n_0) = g(n_0) + h(n_0) = h(n_0)$  with  $n_0 = s$ .
  - > Expand nodes in a DFS fashion—backtrack whenever the  $f$  value of a successor of an expanded node exceeds the cutoff value.
  - > If this terminates at a goal node, then you have a minimal path, else the cost of an optimal path must exceed the cutoff value.
  - > Use as your next cutoff value the value of a node visited but not expanded
  - > IDA\* does have to repeat node expansions, but there are potential tradeoffs involving reduced memory requirements and ease of implementation

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**Performance Issues**

**Penetrance**

- The penetrance  $P$  of a search algorithm measures the extent to which the search focuses toward a goal and does not wander off  
 $P = L/T$  where  $L$  = length of a found path to the goal  
 $T$  = total number of nodes (excluding  $s$ )  
 $P_{max} = 1$   $P$  is a function (difficulty, efficiency of search)  
 $T$  grows faster than  $L$  and thusly  $P$  is usually high for small  $L$  and small for large  $L$   
 $P$  measures when a tree is elongated vs bushy

**Branching Factor**

- The branching factor  $B$  is based on a tree having
  - > depth equal to path length
  - > a total number of nodes = to the nodes generated during search
  - $B$  measures the constant number of successors of each node in such a tree

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